

March 7, 1984

WOCOMAL FRESHMAN MEET

ROUND I: ALGEBRAIC WORD PROBLEMS

ALL ANSWERS MUST BE EXPRESSED IN SIMPLEST EXACT FORM

1. The second angle of a triangle measures three times the first angle. The third angle measures  $80^\circ$  more than the first angle. Find the measure of the largest angle.
  
  
  
  
  
  
  
  
  
  
2. How many ounces of water must be evaporated from 16 ounces of a 25% salt solution to obtain a 40% solution?
  
  
  
  
  
  
  
  
  
  
3. A, B, C are points in this order on a road. On Monday a motorist covers the distance AB at a speed of 36 miles per hour and BC at 24 miles per hour, taking 2 hours and 50 minutes for the entire trip. On Tuesday he covers the entire distance at 30 miles per hour, taking 2 hours and 48 minutes. Find the distance BC.

ANSWERS: (1 point) 1. \_\_\_\_\_

(2 points) 2. \_\_\_\_\_ ounces

(3 points) 3. \_\_\_\_\_ miles

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ROUND II: SET THEORY

ALL ANSWERS MUST BE EXPRESSED IN SIMPLEST FORM

1. If  $A = \{0, 1, 5, 6, 7, 9\}$   
 $B = \{2, 3, 6, 7, 8, 9\}$   
 $C = \{4, 5, 6, 8\}$   
find  $(A \cap B) \cup (A \cap C)$ .

2.  $A \cap B$  has 8 subsets.  $A \cup B$  has 32 subsets. If sets A and B are in a one-to-one correspondence, how many subsets of set B are there?

- . 88 students competed in the last WOCOMAL round.  
4 students got a perfect score.  
3 students got only question 1 wrong.  
6 students got only question 2 wrong.  
14 students got only question 3 wrong.  
52 students got question 1 right.  
37 students got question 2 right.  
15 students got question 3 right.  
How many students got a score of zero?

ANSWERS: (1 point) 1. \_\_\_\_\_

(2 points) 2. \_\_\_\_\_

(3 points) 3. \_\_\_\_\_

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ROUND III: OPEN

ALL ANSWERS MUST BE EXPRESSED IN SIMPLEST EXACT FORM

1. The sum of a number, its half, its third and its fourth equals 100.  
What is the number?
2. If  $12 \text{ Hinkles} = 5 \text{ Dinkles}$  and  $3 \text{ Dinkles} = 4 \text{ Sprinkles}$ ,  
then how many Sprinkles are there in 4 Hinkles?
3. The same test is given to three math classes. The first, a class  
of twenty, averages 80. The second, a class of thirty, averages  
70. What average must the third class, consisting of twenty-five  
students, get so that the over-all average of all the students  
is 75?

ANSWERS: (1 point) 1. \_\_\_\_\_

(2 points) 2. \_\_\_\_\_

(3 points) 3. \_\_\_\_\_

Assabet Valley, Hudson, Notre Dame

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ROUND IV: OPERATIONS ON POLYNOMIALS

ALL ANSWERS MUST BE EXPRESSED IN SIMPLEST FORM

1. From the sum of  $6x^2 - 5x - 7$  and  $8 - 7x^2$  subtract the difference of  $6 - 8x - x^2$  minus  $7x - 11$ .

2. The scores of several tests totaled  $x^3 + 7x^2 + 4x - 12$ . The average score was  $x^2 + 8x + 12$ . How many tests were there?

3. Simplify:  $2a^2 - 3(a + 1)(a - 2) - 7[-(a - 1)]^2$ .

ANSWERS: (1 point) 1. \_\_\_\_\_

(2 points) 2. \_\_\_\_\_

(3 points) 3. \_\_\_\_\_

Saint John's, Shepherd Hill, Tantasqua

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WOCOMAL FRESHMAN MEET

TEAM ROUND: FACTORING

EACH QUESTION IS WORTH THREE POINTS

FACTOR COMPLETELY AND SIMPLIFY EACH FACTOR WHEN POSSIBLE

1.  $60y^2 - 140y + 40$

1. \_\_\_\_\_

2.  $m^2 - 1 - n^2 + 2n$

2. \_\_\_\_\_

3.  $3x^3y^2 - 6x^2y^2 + 6xy^2$

3. \_\_\_\_\_

4.  $3x(18x^2 - 2) - 18x^2 + 2$

4. \_\_\_\_\_

5.  $7a^3 + 49a^2 + 84a$

5. \_\_\_\_\_

6.  $x^2 - 4y^2 + x + 2y$

6. \_\_\_\_\_

7.  $b^4 - 13b^2 + 36$

7. \_\_\_\_\_

8.  $x^2y + x^2 - 9y - 9$

8. \_\_\_\_\_

Auburn, Bartlett, Bromfield, Leicester,  
Notre Dame, Quaboag, Shrewsbury, Southbridge

March 7, 1984

WOCOMAL FRESHMAN MEET ANSWERS

ROUND I

- (1 point) 1. 100 or  $100^\circ$   
(2 points) 2. 6 ounces  
(3 points) 3. 36 miles

TEAM ROUND

(3 points each)

1.  $20(3y - 1)(y - 2)$   
2.  $(m + n - 1)(m - n + 1)$

ROUND II

- (1 point) 1. {5, 6, 7, 9}  
(2 points) 2. 16  
(3 points) 3. 15

3.  $3xy^2(x^2 - 2x + 2)$   
4.  $2(3x + 1)(3x - 1)(3x - 1)$   
or  $2(3x + 1)(3x - 1)^2$

ROUND III

- (1 point) 1. 48  
(2 points) 2.  $\frac{20}{9}$  or  $2\frac{2}{9}$  or  $2.\bar{2}$   
(3 points) 3. 77

5.  $7a(a + 4)(a + 3)$   
6.  $(x + 2y)(x - 2y + 1)$

ROUND IV

- (1 point) 1.  $10x - 16$   
(2 points) 2.  $x - 1$   
(3 points) 3.  $-8a^2 + 17a - 1$

7.  $(b + 2)(b - 2)(b + 3)(b - 3)$   
8.  $(y + 1)(x + 3)(x - 3)$